# Descriptive Statistics 

## Descriptive Statistics

- Data we are facing today
- Scale of data has become larger and larger
- Dimensionality increased
- Descriptive statistics is the first step statisticians do with their data
- Understand your data
- Draw some hypothesis

Daily vitamin-A consumption among cancer cases and controls


*RDA $=$ Recommended Daily Allowance.

## Common statistical terms

- Data
- Variables
- A characteristic that is observed or manipulated
- Can take on different values
- Values


## Statistical terms (cont.)

- Independent variables
- Precede dependent variables in time
- Are often manipulated by the researcher
- The treatment or intervention that is used in a study
- Dependent variables
- What is measured as an outcome in a study
- Values depend on the independent variable


## Statistical terms (cont.)

- Parameters
- Summary data from a population
- Statistics
- Summary data from a sample


## Populations

- A population is the group from which a sample is drawn
- e.g., headache patients in a doctor's office; automobile crash victims in an emergency room
- In research, it is not practical to include all members of a population
- Thus, a sample (a subset of a population) is taken


## Random samples

- Subjects are selected from a population so that each individual has an equal chance of being selected
- Random samples are representative of the source population
- Non-random samples are not representative
- May be biased regarding age, severity of the condition, socioeconomic status etc.


## Descriptive statistics (DSs)

- A way to summarize data from a sample or a population
- DSs illustrate the shape, central tendency, and variability of a set of data
- The shape of data has to do with the frequencies of the values of observations
- Central tendency describes the location of the middle of the data
- Variability is the extent values are spread above and below the middle values
- a.k.a., Dispersion


## Hypothetical study data

- Distribution provides a summary of:
- Frequencies of each of the values

Case \# Visits

- 2-3

17
22

- 3-4

32
43

- 4-3
- 5-1
- 6-1
- 7-2

54
63
75
83
94
106

- Ranges of values
- Lowest $=2$
- Highest $=7$


## Frequency distributions are often depicted by a histogram



## Measures of central tendency

- Mean (a.k.a., average)
- The most commonly used DS
- To calculate the mean
- Add all values of a series of numbers and then divided by the total number of elements


## Formula to calculate the mean

- Mean of a sample

$$
\bar{X}=\frac{\Sigma X}{n}
$$

- Mean of a population $\mu=\frac{\Sigma X}{N}$


## Measures of central tendency (cont.)

- Mode
- The most frequently occurring value in a series
- The modal value is the highest bar in a histogram



## Measures of central tendency (cont.)

- Median
- The value that divides a series of values in half when they are all listed in order
- When there are an odd number of values
- The median is the middle value
- When there are an even number of values
- Count from each end of the series toward the middle and then average the 2 middle values


## Measures of central tendency (cont.)

- Each of the three methods of measuring central tendency has certain advantages and disadvantages
- Which method should be used?
- It depends on the type of data that is being analyzed
- e.g., categorical, continuous, and the level of measurement that is involved


## Levels of measurement

- There are 4 levels of measurement
- Nominal, ordinal, interval, and ratio

1. Nominal

- Data are coded by a number, name, or letter that is assigned to a category or group
- Examples
- Gender (e.g., male, female)
- Treatment preference (e.g., manipulation, mobilization, massage)


## Levels of measurement (cont.)

## 2. Ordinal

- Is similar to nominal because the measurements involve categories
- However, the categories are ordered by rank
- Examples
- Pain level (e.g., mild, moderate, severe)
- Military rank (e.g., lieutenant, captain, major, colonel, general)


## Levels of measurement (cont.)

- Ordinal values only describe order, not quantity
- Thus, severe pain is not the same as 2 times mild pain
- The only mathematical operations allowed for nominal and ordinal data are counting of categories
- e.g., 25 males and 30 females


## Levels of measurement (cont.)

3. Interval

- Measurements are ordered (like ordinal data)
- Have equal intervals
- Does not have a true zero
- Examples
- The Fahrenheit scale, where $0^{\circ}$ does not correspond to an absence of heat (no true zero)
- In contrast to Kelvin, which does have a true zero


## Levels of measurement (cont.)

4. Ratio

- Measurements have equal intervals
- There is a true zero
- Ratio is the most advanced level of measurement, which can handle most types of mathematical operations


## Levels of measurement (cont.)

| Measurement scale | Permissible mathematic <br> operations | Best measure of <br> central tendency |
| :---: | :---: | :---: |
| Nominal | Counting | Mode |
| Ordinal | Greater or less than <br> operations | Median |
| Interval | Addition and subtraction | Symmetrical - Mean <br> Skewed - Median |
| Ratio | Addition, subtraction, <br> multiplication and division | Symmetrical - Mean <br> Skewed - Median |

## The shape of data

- Histograms of frequency distributions have shape
- Distributions are often symmetrical with most scores falling in the middle and fewer toward the extremes
- Many biological data are symmetrically distributed and form a normal curve (a.k.a, bell-shaped curve)


## The shape of data (cont.)



## The shape of data (cont.)



## The normal distribution

- The area under a normal curve has a normal distribution (a.k.a., Gaussian distribution)
- Properties of a normal distribution
- It is symmetric about its mean
- The highest point is at its mean
- The height of the curve decreases as one moves away from the mean in either direction, approaching, but never reaching zero


## The normal distribution (cont.)



## The normal distribution (cont.)



## The normal distribution (cont.)



## The normal distribution (cont.)



## The normal distribution (cont.)



## The normal distribution (cont.)



## The normal distribution (cont.)



## Skewed distributions

- The data are not distributed symmetrically in skewed distributions
- Consequently, the mean, median, and mode are not equal and are in different positions
- Values are clustered at one end of the distribution
- A small number of extreme values are located in the limits of the opposite end


## Skewed distributions (cont.)

- Skew is always toward the direction of the longer tail
- Positive if skewed to the right
- Negative if to the left


Negatively skewed distribution

## Skewed distributions (cont.)

- Because the mean is shifted so much, it is not the best estimate of the average score for skewed distributions
- The median is a better estimate of the center of skewed distributions
- It will be the central point of any distribution
- $50 \%$ of the values are above and $50 \%$ below the median


## Measures of Spread

- Cholesterol measurement
- Variability or spread of the data

Figure 2.4 Two samples of cholesterol measurements on a given person using an Autoanalyzer and a Microenzymatic measurement technique


## Two-number Summary - Variance and Standard Deviation

- Range
- the difference between the largest and smallest observations in a sample.
- Variance

$$
s^{2}=\frac{\sum_{i=1}^{n}\left(x_{i}-\bar{x}\right)^{2}}{n-1}
$$

- Standard deviation

$$
s=\sqrt{\frac{\sum_{i=1}^{n}\left(x_{i}-\bar{x}\right)^{2}}{n-1}}
$$

- SD is the average amount of spread in a distribution of scores
- Example: Pulmonary Disease

The relationship between passive smoking and pulmonary function.
As supporting evidence, the CO concentration in working environments of passive smokers and of nonsmokers.

- If the relative CO concentration changed over the course of the day.

Figure 2.2 Mean carbon-monoxide concentration ( $\pm$ standard error) by time of day as measured in the working environment of passive smokers and nonsmokers who work in nonsmoking environments


Source: Reproduced with permission of The New England Journal of Medicine, 302, 720-723, 1980.

## Case Study: The Scottish Heart Health Study (SHHS)

- Scotland's annual mortality rate from coronary heart disease (CHD) is one of the highest in the world.
- Establishment of Cardiovascular Epidemiology Unit at University of Dundee
- Objectives of SHHS:
- To establish the levels of CHD risk factors in a crosssectional sample of Scottish men and women aged 40-59.
- To determine the extent to which the geographical variation in CHD can be explained in terms of the geographical variation in risk factor levels.
- To assess the relative contribution of the established risk factors, as well as some more recently described ones.


## Case Study: The Scottish Heart Health Study (SHHS) cont.

- Subjects sampled from 22 of the 56 mainland Scottish local government districts.
- From each district, an equal number of people were selected in the four age/sex groups: male 40-49, female 40-49, male 50-59, and female 50-59.
- A questionnaire and an invitation to a local clinic.
- Questionnaire include questions like age, sex, marital status, employment, past medical history, exercise, diet and smoking...
- In clinic visit, height, weight, blood pressure were recorded and a 12-lead electrocardiogram was administered. A blood sample was taken from which serum total cholesterol, fibrinogen, and several other biochemical variables were measured.
- The sample size is 10,359 ( 5123 men and 5236 women).
- The data set comprised 315 variables totally.


# Case Study: The Scottish Heart Health Study (SHHS) cont. 

- Prevalence data are not ideal to demonstrate causality.
- SHHS was designed as a two-phase study.
- The cross-sectional baseline study.
- Follow-up cohort study of several years' duration.
- The follow-up study
- Death registration certificates collected
- Hospital records
-8 years


## Types of Variables

- Qualitative variables
- Categorical variables
- Binary variables
- Ordinal variables (ordered categorical variables)
- Responses like poor/satisfactory/good
- Quantitative variables
- Discrete
- Continuous


## Tables and Charts

- For a single qualitative variable
- Frequency table, bar chart and pie chart

| Table 2.1. Occupational social class in the |  |  |  |
| :--- | :--- | :---: | ---: |
| SHHS. |  |  |  |
| Social class | Number | (\%) |  |
| I | nonmanual, professional | 592 | $(7)$ |
| II | nonmanual, intermediate | 2954 | $(26)$ |
| IIIn | nonmanual, skilled | 1017 | $(12)$ |
| IIIm | manual, skilled | 3150 | $(36)$ |
| IV | manual, partially skilled | 1553 | $(44)$ |
| V | manual, unskilled | 415 | $(5)$ |
| Total |  | 8681 |  |

## Bar Chart



## Pie Chart



Pie chart for occupational social class in the SHHS.

## Comparing Two Qualitative Variables

Table 2.2. Social class by prevalent CHD status in the SHHS.

| Social | Prevalent CHD |  |  |
| :--- | :---: | ---: | ---: |
| class | Yes (\%) | No | Total |
| I | $100(16.9)$ | 492 | 592 |
| II | $382(17.0)$ | 1872 | 2254 |
| IIIn | $183(18.0)$ | 834 | 1017 |
| IIIm | $668(21.2)$ | 2482 | 3150 |
| IV | $279(22.3)$ | 974 | 1253 |
| V | $109(26.3)$ | 306 | 415 |
| Total | $1721(19.8)$ | 6960 | 8681 |

## Bar Chart



| E | CHD |
| :--- | :--- |
| ت | No CHD |

Figure 2.3. Bar chart for occupational social class in the SHHS, showing percentage by CHD status.

## How to Make Good Tables

- Each table should be self-explanatory.
- Each table should have an attractive appearance.
- The rows and columns should be arranged in a natural order.
- Numbers are easier to compare when the table has a vertical orientation.
- Tables should have consistent appearance throughout the report.

Table 2.3. Minimum, median and maximum values for selected variables in developed countries, 1970.

| Variable | Minimum | Median | Maximum |
| :--- | :---: | :---: | :---: |
| Gross national product per person | 1949 | 4236 | 6652 |
| Population per $\mathrm{km}^{2}$ | 1.6 | 77.2 | 324.2 |
| Cigarette consumption per person per year | 630 | 2440 | 3810 |
| Infant mortality per 1000 births | 11.0 | 18.2 | 29.6 |

Source: Cochrane, A.L. et al. (1978), J. Epidemiol. Comm. Health, 32, 200-205.

Table 2.4. Minimum, median and maximum values for selected variables in developed countries, 1970.

|  | Gross <br> national <br> product <br> per person | Population <br> density <br> per $\mathrm{km}^{2}$ | Cigarette <br> consumption per <br> person/per year | Infant <br> mortality rate <br> per 1000 births |
| :--- | :---: | :---: | :---: | :---: |
| Maximum | 6652 | 324.2 | 3810 | 29.6 |
| Median | 4236 | 77.2 | 2440 | 18.2 |
| Minimum | 1949 | 1.6 | 630 | 11.0 |

Table 2.5. Smoking habit by diagnosis group by sex.

|  | CHD diagnosis group |  |  |  |  |
| :--- | ---: | ---: | ---: | ---: | ---: |
| Sex/smoking habit | Diagnosed | Control | Undiagnosed | Total |  |
| Males |  |  |  |  |  |
| Solely cigarette | $125(8 \%)$ | 1175 | $(77 \%)$ | $226(15 \%)$ | 1526 |
| Solely cigar | $25(7 \%)$ | 313 | $(83 \%)$ | $40(10 \%)$ | 378 |
| Solely pipe | $9(8 \%)$ | 80 | $(72 \%)$ | $22(20 \%)$ | 111 |
| Mixed smokers | $39(8 \%)$ | 379 | $(75 \%)$ | $89(17 \%)$ | 507 |
| All smokers | $198(8 \%)$ | 1947 | $(77 \%)$ | $377(15 \%)$ | 2522 |
|  |  |  |  |  |  |
| Females |  |  |  |  |  |
| Solely cigarette | $105(6 \%)$ | 1410 | $(78 \%)$ | $297(16 \%)$ | 1812 |
| Solely cigar | 0 | $12(100 \%)$ | 0 | 12 |  |
| Mixed smokers | $2(8 \%)$ | 20 | $(77 \%)$ | $4(15 \%)$ | 26 |
| All smokers | $107(6 \%)$ | 1442 | $(78 \%)$ | $301(16 \%)$ | 1850 |

${ }^{\text {a }}$ No females smoked a pipe.
Table 2.6. Diagnosis group by previous smoking habit by sex for nonsmokers.

| CHD <br> diagnosis group | Males |  |  | Females |  |  |
| :--- | :---: | :---: | :---: | :---: | ---: | :---: |
|  | Ex-smokers | Never-smokers |  | Ex-smokers | Never-smokers |  |
| Diagnosed | $142(11 \%)$ | $45(4 \%)$ |  | $58(6 \%)$ | $75(4 \%)$ |  |
| Control | $993(76 \%)$ | $888(83 \%)$ |  | $767(80 \%)$ | $1581(78 \%)$ |  |
| Undiagnosed | $164(13 \%)$ | $143(13 \%)$ |  | $137(14 \%)$ | $375(18 \%)$ |  |

Table 2.7. Men and women classified by self-declared smoking habit and diagnosis group.

| Sex/smoking habit | CHD diagnosis group |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Diagnosed |  | Undiagnosed |  | Control |  |
| Males |  |  |  |  |  |  |
| Solely cigarettes | 125 | (32\%) | 226 | (33\%) | 1175 | (31\%) |
| Solely cigars | 25 | (7\%) | 40 | (6\%) | 313 | (8\%) |
| Solely pipes | 9 | (2\%) | 22 | (3\%) | 80 | (2\%) |
| Mixed smokers | 39 | (10\%) | 89 | (13\%) | 379 | (10\%) |
| Ex-smokers (of any) | 142 | (37\%) | 164 | (24\%) | 993 | (26\%) |
| Never-smokers (of any) | 45 | (12\%) | 143 | (21\%) | 888 | (23\%) |
| Total | 385 (100\%) |  | 684 (100\%) |  | 3828 (100\%) |  |
| Females - |  |  |  |  |  |  |
| Solely cigarettes | 105 | (44\%) | 297 | (37\%) | 1410 | (37\%) |
| Solely cigars | 0 |  | 0 |  | 12 | (0\%) |
| Mixed smokers | 2 | (1\%) | 4 | (0\%) | 20 | (1\%) |
| Ex-smokers (of any) | 58 | (24\%) | 137 | (17\%) | 767 | (20\%) |
| Never-smokers (of any) | 75 | (31\%) | 375 | (46\%) | 1581 | (42\%) |
| Total | 240 | (100\%) | 813 | (100\%) | 3790 | (100\%) |

Note: Percentages less than $0.5 \%$ are given as $0 \%$.
Source: Woodward, M. and Tunstall-Pedoe, H. (1992), Eur. Heart J., 13, 160-165.

## Descriptive Techniques for Quantitative Variables

- Numerical summarization
- More important in report writing
- Economical in space
- Pictorial shape investigation
- More important in initial exploration
- Many analytical techniques are only suitable for data of a certain shape

