## Problem I

The data in Table 6.8 concern the mean triceps skin-fold thickness in a group of normal men and a group of men with chronic airflow limitation.

| Table 6.8 <br> Triceps skin-fold thickness in normal men <br> and men with chronic airflow limitation |
| :--- |
| Group |
| Mean |
| Normal |
| Chronic airflow limitation |

1. What is the standard error of the mean for each group?
2. Assume that the central-limit theorem is applicable. What does it mean in this context?
3. Find the upper 1st percentile of a t distribution with 16 df .
4. Find the lower 10th percentile of a t distribution with 28 df .

5 . Find the upper 2.5 th percentile of a t distribution with 7 df .
6. What are the upper and lower 2.5 th percentiles for a chi-square distribution with 2 df ? What notation is used to denote these percentiles?

## Problem II

Consider the hospital stay data below. Also find the link in the webpage
http://www.stat.fsu.edu/~debdeep/hospital.txt

Table 2.11 Hospital-stay data

| $\begin{aligned} & \text { ID } \\ & \text { no. } \end{aligned}$ | Duration of hospital stay | Age | $\begin{gathered} \text { Sex } \\ 1=M \\ 2=F \end{gathered}$ | First temp. following admission | First WBC (× $10^{3}$ ) following admission | Received antibiotic $\begin{aligned} & 1=\text { yes } \\ & 2=\text { no } \end{aligned}$ | Received bacterial culture 1 = yes $2=$ no | $\begin{aligned} & \text { Service } \\ & 1=\text { med. } \\ & 2=\text { surg. } \end{aligned}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 5 | 30 | 2 | 99.0 | 8 | 2 | 2 | 1 |
| 2 | 10 | 73 | 2 | 98.0 | 5 | 2 | 1 | 1 |
| 3 | 6 | 40 | 2 | 99.0 | 12 | 2 | 2 | 2 |
| 4 | 11 | 47 | 2 | 98.2 | 4 | 2 | 2 | 2 |
| 5 | 5 | 25 | 2 | 98.5 | 11 | 2 | 2 | 2 |
| 6 | 14 | 82 | 1 | 96.8 | 6 | 1 | 2 | 2 |
| 7 | 30 | 60 | 1 | 99.5 | 8 | 1 | 1 | 1 |
| 8 | 11 | 56 | 2 | 98.6 | 7 | 2 | 2 | 1 |
| 9 | 17 | 43 | 2 | 98.0 | 7 | 2 | 2 | 1 |
| 10 | 3 | 50 | 1 | 98.0 | 12 | 2 | 1 | 2 |
| 11 | 9 | 59 | 2 | 97.6 | 7 | 2 | 1 | 1 |
| 12 | 3 | 4 | 1 | 97.8 | 3 | 2 | 2 | 2 |
| 13 | 8 | 22 | 2 | 99.5 | 11 | 1 | 2 | 2 |
| 14 | 8 | 33 | 2 | 98.4 | 14 | 1 | 1 | 2 |
| 15 | 5 | 20 | 2 | 98.4 | 11 | 2 | 1 | 2 |
| 16 | 5 | 32 | 1 | 99.0 | 9 | 2 | 2 | 2 |
| 17 | 7 | 36 | 1 | 99.2 | 6 | 1 | 2 | 2 |
| 18 | 4 | 69 | 1 | 98.0 | 6 | 2 | 2 | 2 |
| 19 | 3 | 47 | 1 | 97.0 | 5 | 1 | 2 | 1 |
| 20 | 7 | 22 | 1 | 98.2 | 6 | 2 | 2 | 2 |
| 21 | 9 | 11 | 1 | 98.2 | 10 | 2 | 2 | 2 |
| 22 | 11 | 19 | 1 | 98.6 | 14 | 1 | 2 | 2 |
| 23 | 11 | 67 | 2 | 97.6 | 4 | 2 | 2 | 1 |
| 24 | 9 | 43 | 2 | 98.6 | 5 | 2 | 2 | 2 |
| 25 | 4 | 41 | 2 | 98.0 | 5 | 2 | 2 | 1 |

1. Compute a $95 \%$ CI for the mean duration of hospitalization.
2. Compute a $95 \%$ CI for the mean white blood count following admission.
3. Answer Problem 2 for a $90 \%$ CI.
4. What is the relationship between your answers to Problems 2 and 3 ?

## Problem III

Suppose 100 hypertensive people are given an antihypertensive drug and the drug is effective in 20 of them. By effective, we mean their DBP is lowered by at least 10 mm Hg as judged from a repeat blood-pressure measurement 1 month after taking the drug.

1. What is the best point estimate of the probability p of the drug being effective?
2. A placebo is a simulated or otherwise medically ineffectual treatment for a disease or other medical condition intended to deceive the recipient. Sometimes patients given a placebo treatment will have a perceived or actual improvement in a medical condition, a phenomenon commonly called the placebo effect. Suppose we know that $10 \%$ of all hypertensive patients who are given a placebo will have their DBP lowered by 10 mm Hg after 1 month. Can we carry out some procedure to be sure we are not simply observing the placebo effect?
3. What assumptions have you made to carry out the procedure in the previous question?
4. Suppose we decide a better measure of the effectiveness of the drug is the mean decrease in blood pressure rather than the measure of effectiveness used previously. Let $d_{i}=x_{i}-y_{i}, i=1, \ldots, 100$ where $x_{i}=$ DBP for the $i$ th person before taking the drug and $y_{i}=$ DBP for the $i$ th person 1 month after taking the drug. Suppose the sample mean of the $d_{i}$ is +5.3 and the sample variance is 144.0 .
5. What is the standard error of $d$ ?
6. What is a $95 \%$ CI for the population mean of $d$ ?
7. Can we make a statement about the effectiveness of the drug?
8. What does a $95 \%$ CI mean, in words, in this case?
