

Test #3 will be on Wednesday, April 22.

Exercise: Find the Fisher information matrix for a k -parameter exponential family with the natural parameter $w(\theta) = \theta$.

Read Sections 8.1, 8.2.1, 8.3.1 (skip example 8.3.8), 8.3.2, and 10.3.1 (stop at the beginning of example 10.3.4).

Do problems 8.3, 8.5, 8.6, 8.15, 8.20.

Comment on Problem 8.5(c):

There are a few ways you can do this. Here is one. If we set $\theta = 1$, the Pareto family becomes a scale family in the parameter ν . Since T is scale invariant, the distribution of T (when $\theta = 1$) does not depend on the value of ν . Thus we can also set $\nu = 1$ without loss of generality. Now check that if X is Pareto with $\theta = 1$ and $\nu = 1$, then $Y = \log(X)$ has an exponential distribution with mean 1. This allows you to find the distribution of $\log(T)$ using the memoryless property of the exponential distribution: $T = \sum [\log(X_i) - \log(\min X_i)]$ and each of the nonzero terms in this sum has an exponential distribution with mean one. (This is just an informal argument.) Thus $\log(T)$ has a $\text{gamma}(n-1, 1)$ distribution.